

Signature of Invigilators

Roll No.

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(In figures as in Admit Card)

1.

2.

PHYSICAL SCIENCES

Paper III

Roll No.

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(In words)

D—0202

Name of Areas/Section (if any)

Time Allowed : 2½ Hours]

[Maximum Marks : 200

Instructions for the Candidates

FOR OFFICE USE ONLY Marks Obtained

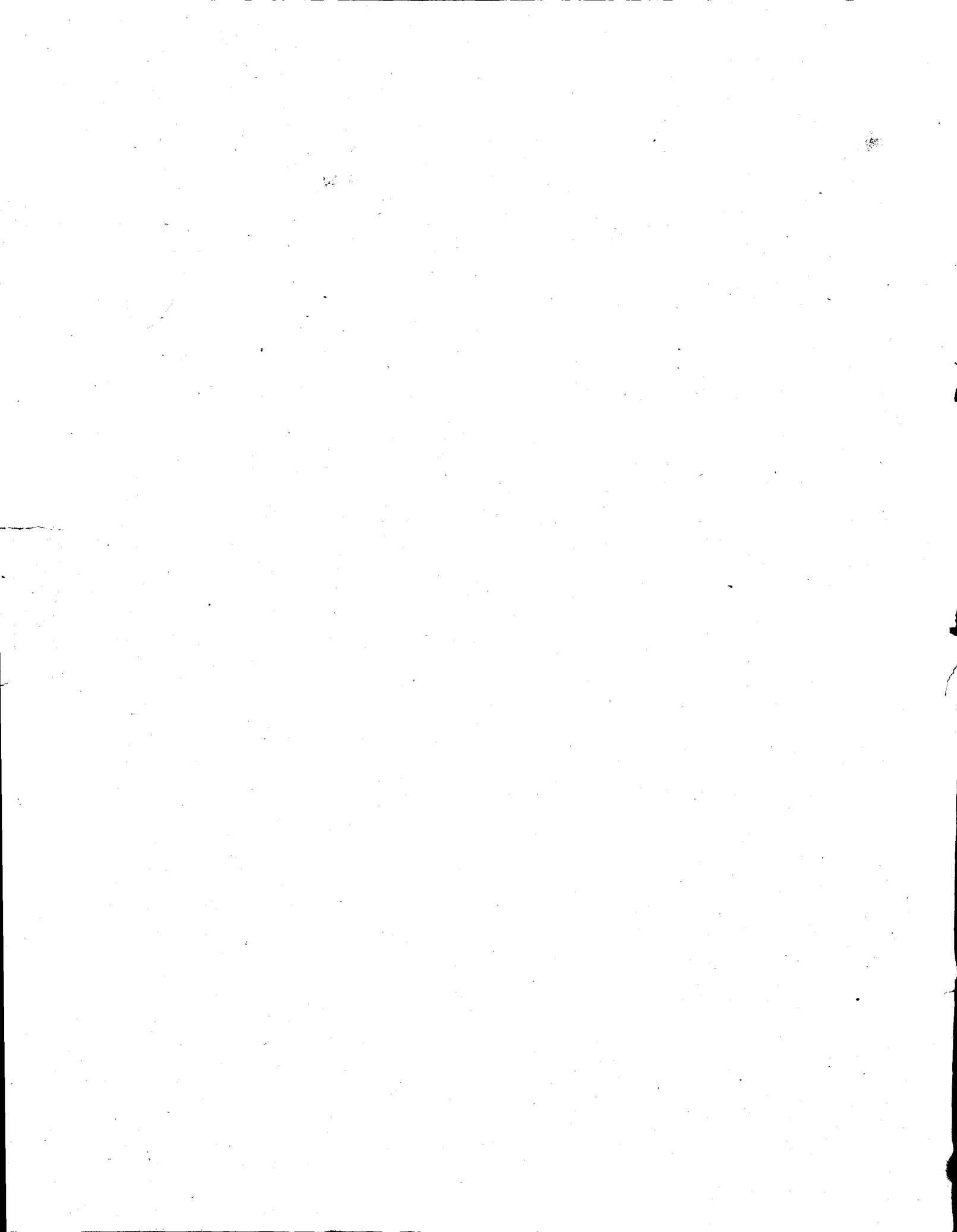
Question Number	Marks Obtained	Question Number	Marks Obtained	Question Number	Marks Obtained
1		26			
2					
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Total Marks Obtained.....
Signature of the co-ordinator.....
(Evaluation)

1. Write your Roll number in the space provided on the top of this page.
2. Write name of your Elective/Section if any.
3. Answer to short answer/essay type questions are to be written in the space provided below each question or after the questions in test booklet itself. No additional sheets are to be used.
4. Read instructions given inside carefully.
5. Last page is attached at the end of the test booklet for rough work.
6. If you write your name or put any special mark on any part of the test booklet which may disclose in any way your identity, you will render yourself liable to disqualification.
7. Use of calculator or any other Electronics Devices are prohibited.
8. There is no negative marking.
9. You should return the test booklet to the invigilator at the end of the examination and should not carry any paper outside the examination hall.

પરીક્ષાર્થીઓ માટે સૂચનાઓ :

૧. આ પૃષ્ઠના ઉપલા ભાગે આપેલી જગ્યામાં તમારી ક્રમાંક સંખ્યા (રોલ નંબર) લખો.
૨. તમે જે વિકલ્પનો ઉત્તર આપો તેનો સ્પષ્ટ નિર્દેશ કરો.
૩. ટૂંક નોંધ કે નિબંધ પ્રકારના પ્રશ્નોના ઉત્તર દરેક પ્રશ્નની નીચે આપેલી જગ્યામાં જ લખો. વધારાના કોઈ કાગળનો ઉપયોગ કરશો નહીં.
૪. અંદર આપેલી સૂચનાઓ ધ્યાનથી વાંચો.
૫. આ ઉત્તરપોથીને અંતે આપેલું પૃષ્ઠ કાચા કામ માટે છે.
૬. આ ઉત્તરપોથીમાં કયાંય પણ તમારી ઓળખ કરાવી દે એવી રીતે તમારું નામ કે કોઈ ચોકકસ નિશાની કરી હશે તો તમે આ પરીક્ષા માટે ગેરલાયક સાબીત થશો.
૭. કેલક્યુલેટર અથવા ઈલેક્ટ્રોનિક્સ સાધનો જેવા ઉપયોગ કરવો નહીં.
૮. નકારાત્મક ગુણાંક પદ્ધતિ નથી.
૯. પ્રશ્નપત્ર લખાઈ રહે એટલે આ ઉત્તરપોથી તમારા નિરીક્ષકને આપી દેવી. પરીક્ષાખંડની બહાર કોઈપણ પ્રશ્નપત્ર લઈ જવું નહીં.



LOGARITHMS

0	0000	0043	0086	0128	0170	0212	0253	0294	0334	0374	59 13	17 21	30 34	43 38
10	0414	0453	0492	0531	0569	0607	0645	0682	0719	0755	48 12	16 20	28 22	41 30
20	0801	0838	0874	0909	0944	0979	1014	1048	1082	1116	47 11	15 18	26 20	39 33
30	1153	1189	1224	1259	1293	1327	1361	1395	1429	1463	37 11	14 18	25 28	37 31
40	1501	1536	1571	1605	1639	1673	1707	1741	1775	1809	36 9	13 16	24 27	35 29
50	1853	1887	1921	1955	1989	2023	2057	2091	2125	2159	36 8	12 14	23 26	34 30
60	2201	2235	2269	2303	2337	2371	2405	2439	2473	2507	36 7	11 14	22 25	33 29
70	2553	2587	2621	2655	2689	2723	2757	2791	2825	2859	36 6	11 14	22 25	33 29
80	2901	2935	2969	3003	3037	3071	3105	3139	3173	3207	36 5	10 13	21 24	32 28
90	3253	3287	3321	3355	3389	3423	3457	3491	3525	3559	36 4	10 13	21 24	32 28
100	3601	3635	3669	3703	3737	3771	3805	3839	3873	3907	36 3	9 12	20 23	31 27
110	3953	3987	4021	4055	4089	4123	4157	4191	4225	4259	36 2	9 12	20 23	31 27
120	4301	4335	4369	4403	4437	4471	4505	4539	4573	4607	36 1	8 10	19 22	30 26
130	4653	4687	4721	4755	4789	4823	4857	4891	4925	4959	35 8	8 10	19 22	30 26
140	5001	5035	5069	5103	5137	5171	5205	5239	5273	5307	35 7	7 9	18 21	29 25
150	5353	5387	5421	5455	5489	5523	5557	5591	5625	5659	35 6	7 9	18 21	29 25
160	5701	5735	5769	5803	5837	5871	5905	5939	5973	6007	35 5	6 8	17 20	28 24
170	6053	6087	6121	6155	6189	6223	6257	6291	6325	6359	35 4	6 8	17 20	28 24
180	6401	6435	6469	6503	6537	6571	6605	6639	6673	6707	35 3	5 7	16 19	27 23
190	6753	6787	6821	6855	6889	6923	6957	6991	7025	7059	35 2	5 7	16 19	27 23
200	7101	7135	7169	7203	7237	7271	7305	7339	7373	7407	35 1	4 6	15 18	26 22
210	7453	7487	7521	7555	7589	7623	7657	7691	7725	7759	34 9	4 6	15 18	26 22
220	7801	7835	7869	7903	7937	7971	8005	8039	8073	8107	34 8	3 5	14 17	25 21
230	8153	8187	8221	8255	8289	8323	8357	8391	8425	8459	34 7	3 5	14 17	25 21
240	8501	8535	8569	8603	8637	8671	8705	8739	8773	8807	34 6	3 5	14 17	25 21
250	8853	8887	8921	8955	8989	9023	9057	9091	9125	9159	34 5	2 4	13 16	24 20
260	9201	9235	9269	9303	9337	9371	9405	9439	9473	9507	34 4	2 4	13 16	24 20
270	9553	9587	9621	9655	9689	9723	9757	9791	9825	9859	34 3	2 4	13 16	24 20
280	9901	9935	9969	10003	10037	10071	10105	10139	10173	10207	34 2	1 3	12 15	23 19
290	10253	10287	10321	10355	10389	10423	10457	10491	10525	10559	34 1	1 3	12 15	23 19

LOGARITHMS

50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067	123	345	678
51	7070	7084	7093	7101	7110	7118	7126	7135	7143	7152	123	345	678
52	7160	7177	7185	7193	7202	7210	7218	7226	7235	7243	122	345	677
53	7243	7251	7259	7267	7275	7284	7292	7300	7308	7316	122	345	677
54	7314	7322	7330	7338	7346	7354	7362	7370	7378	7386	122	345	677
55	7404	7412	7419	7427	7435	7443	7451	7459	7466	7474	122	345	677
56	7482	7490	7497	7505	7513	7521	7529	7536	7543	7551	122	345	677
57	7559	7566	7574	7582	7590	7597	7604	7612	7619	7627	122	345	677
58	7634	7642	7649	7657	7664	7672	7679	7686	7694	7701	122	345	677
59	7709	7716	7723	7731	7738	7745	7752	7760	7767	7774	122	345	677
60	7782	7789	7796	7803	7810	7818	7825	7832	7839	7846	122	345	677
61	7853	7860	7868	7875	7882	7889	7896	7903	7910	7917	122	345	677
62	7924	7931	7938	7945	7952	7959	7966	7973	7980	7987	122	345	677
63	7993	8000	8007	8014	8021	8028	8035	8041	8048	8055	122	345	677
64	8062	8069	8075	8082	8089	8096	8102	8109	8116	8122	122	345	677
65	8129	8136	8142	8149	8156	8162	8169	8176	8182	8189	122	345	677
66	8195	8202	8209	8215	8222	8228	8235	8241	8248	8254	122	345	677
67	8261	8268	8274	8280	8287	8293	8299	8306	8312	8319	122	345	677
68	8325	8331	8338	8344	8351	8357	8363	8370	8376	8382	122	345	677
69	8388	8395	8401	8407	8414	8420	8426	8432	8439	8445	122	345	677
70	8451	8457	8463	8470	8476	8482	8488	8494	8500	8506	122	345	677
71	8513	8519	8525	8531	8537	8543	8549	8555	8561	8567	122	345	677
72	8573	8579	8585	8591	8597	8603	8609	8615	8621	8627	122	345	677
73	8633	8639	8645	8651	8657	8663	8669	8675	8681	8686	122	345	677
74	8692	8698	8704	8710	8716	8722	8727	8733	8739	8745	122	345	677
75	8751	8756	8762	8768	8774	8779	8785	8791	8797	8802	122	345	677
76	8808	8814	8820	8825	8831	8837	8842	8848	8854	8859	122	345	677
77	8865	8871	8876	8882	8887	8893	8899	8904	8910	8915	122	345	677
78	8921	8927	8932	8938	8943	8949	8954	8960	8965	8971	122	345	677
79	8976	8982	8987	8993	8998	9004	9009	9015	9020	9025	122	345	677
80	9031	9036	9042	9047	9053	9058	9063	9069	9074	9079	122	345	677
81	9085	9090	9096	9101	9106	9112	9117	9122	9128	9133	122	345	677
82	9138	9143	9149	9154	9159	9165	9170	9175	9180	9186	122	345	677
83	9191	9196	9201	9206	9212	9217	9222	9227	9232	9238	122	345	677
84	9243	9248	9253	9258	9263	9269	9274	9279	9284	9289	122	345	677
85	9294	9299	9304	9309	9315	9320	9325	9330	9335	9340	122	345	677
86	9345	9350	9355	9360	9365	9370	9375	9380	9385	9390	122	345	677
87	9395	9400	9405	9410	9415	9420	9425	9430	9435	9440	122	345	677
88	9445	9450	9455	9460	9465	9470	9475	9480	9485	9490	122	345	677
89	9494	9499	9504	9509	9513	9518	9523	9528	9533	9538	122	345	677
90	9542	9547	9552	9557	9562	9566	9571	9576	9581	9586	122	345	677
91	9590	9595	9600	9605	9609	9614	9619	9624	9628	9633	122	345	677
92	9638	9643	9647	9652	9657	9661	9666	9671	9675	9680	122	345	677
93	9685	9689	9694	9699	9703	9708	9713	9717	9722	9727	122	345	677
94	9731	9736	9741	9745	9750	9754	9759	9763	9768	9773	122	345	677
95	9777	9782	9787	9791	9795	9800	9805	9809	9814	9818	122	345	677
96	9823	9827	9832	9836	9841	9845	9850	9854	9859	9863	122	345	677
97	9868	9872	9877	9881	9886	9890	9894	9899	9903	9908	122	345	677
98	9912	9917	9921	9926	9930	9934	9939	9943	9948	9952	122	345	677
99	9956	9961	9965	9969	9974	9978	9983	9987	9991	9996	122	345	677

PHYSICAL SCIENCES

PAPER III

- Note* :—(i) Part A consists of 10 questions of 10 marks each. Attempt each question in about 200 words (2 pages). All questions are compulsory.
- (ii) Part B consists of 16 questions of 25 marks each. Attempt any four questions from Part B. Each question is to be answered in about 500 words (5 pages).
- (iii) Log tables are allowed, but not a calculator.

PART A

1. (a) Prove that

$$\vec{\nabla} \times \psi \vec{\nabla} \psi = 0.$$

- (b) Show that $\begin{pmatrix} 0 & 1 & -1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix}$ is a Hermitian matrix. Also find out the eigenvalues and eigen vectors of this matrix.

2. The Lagrangian of a particle of mass m is $L = m\dot{x}\dot{y} - m\omega_0^2 xy$.
- (a) Write down the equations of motion for this system. What is the physical system represented by this Lagrangian? What is the energy E of this system? Express E in terms of coordinates and momenta.
- (b) Find the Hamiltonian H associated with the above L . Compare E and H . Comment on your result.
3. Show that the total scattering cross-section of point particles from a perfectly rigid sphere of radius R is πR^2 .
4. A current I is uniformly distributed over a wire of circular cross-section with

radius R . Find the volume current density \vec{J} . If the current density in this wire is proportional to the distance from the axis, find the total current in the wire and establish the continuity equation

$$\vec{\nabla} \cdot \vec{J} + \frac{\partial \rho}{\partial t} = 0.$$

5. Write down Maxwell's equations for an ohmic conducting medium. Obtain the wave equations satisfied by \vec{E} and \vec{B} . Assuming plane wave solutions of these equations obtain the relation between the propagation vector \vec{k} and the frequency ω of these solutions in terms of the conductivity σ , the permittivity ϵ and permeability μ of the medium. Obtain an expression for the refractive index in terms of ω , ϵ , μ and σ .
6. (a) If the resolving limit of the electron microscope is twice the wavelength of its accelerated electron, find the resolving limit for 60 keV electrons.
- (b) Estimate the ground state energy of Hydrogen atom using Heisenberg uncertainty principle.
7. (a) Applying the variation method estimate the ground state energy of a two-electron atom.

(b) If the total angular momentum of a system is $\vec{J} = \vec{L} + \vec{S}$, prove that

$$[J_x, z] = -i\hbar y \quad \text{and} \quad [J_x, y] = i\hbar z.$$

8. A photon gas confined in a volume V is in thermal equilibrium at temperature T . The photon is a massless particle so that $\epsilon = pc$.

Given that the number of states of photons in volume V with energy between ϵ and $\epsilon + d\epsilon$ is

$$D(\epsilon) d\epsilon = \frac{V}{\pi^2 (\hbar c)^3} \epsilon^2 d\epsilon,$$

obtain the Planck distribution law for the spectral energy density along the following lines :

What is the chemical potential of a photon gas ? Show that the temperature dependence of the average energy, $\langle U \rangle$, of the photon gas is proportional to T^4 .

9. Describe a method to determine crystal structure of a polycrystalline material by X-ray diffraction. If X-rays are to be replaced by neutrons, explain why one has to use thermal neutrons.
10. State the principles of least squares. Describe the procedure of least squares for fitting a straight line to a set of five (x_i) assumed experimental points.

PART B

11. What are different types of transistor biasing ? Give the circuit diagram of a common emitter $n-p-n$ transistor biasing circuit with a fixed bias to the emitter. Using typical numerical values for the different resistances in the circuit and power supply value, calculate the circuit parameters I_B , I_C and V_{CE} .
12. What is a discriminator ? Give the circuit diagram of the Schmidt trigger and discuss its operation. Illustrate with an example how and where it is used.
13. Draw a circuit diagram of a binary 1 bit memory cell using basic gates. In turn using it as building blocks draw the schematic diagram of a series in-parallel out 5 digit shift register. How to convert it into parallel-in parallel-out register ?

14. What are the drawbacks of a basic R-S Flip-Flop ? How are they rectified to get a perfect Master-Slave Flip-Flop ? Explain the development of the stages using the truth tables.
15. NMR is the nuclear analog of ESR. Discuss this statement keeping in view the nuclear spin and magnetic moment, Bohr magneton and Zeeman splitting. Show that the resonance frequency lies in radio frequency range. Nuclear magnetic resonance in water is due to the protons of hydrogen. Calculate the field when the resonance frequency $\nu_r = 60$ MHz.
 [Given : $\mu_B = 5.05 \times 10^{-27}$ ampere . meter², $\mu_P = 2.793 \mu_N$, $I = \frac{1}{2}$].
16. Why is Stark effect more important in molecular spectroscopy than Zeeman effect ? Under what condition the first order Stark effect is observed ? Obtain the expression for energies and discuss the selection rules.
17. Discuss the L-S coupling. How does it lead to Hund's rule ? State the Hund's rules and illustrate the applications of these rules.
18. In spite of having equal probabilities for the absorption and the stimulated emission in a two level system we do not generally observe the latter. Why ? What must we do to observe it ? What are different techniques to achieve it ? Is it a sufficient condition for lasing ? If not, how one can obtain lasing in He-Ne laser ?
19. In dielectric materials effect of polarization reduces the field while in case of ferromagnetic materials effect of polarization increases the field. Discuss.
20. Discuss the salient features of BCS theory. How one can explain Josephson effect on the basis of this theory ?

21. Derive expression for specific heat at constant volume due to the free electrons in metals. Calculate the temperature at which the electronic contribution to C_v of silver eventually become identical to the Dulong-Petit value. E_F and N_F for silver are 5 eV and 10^{28} respectively.
22. Explain the construction of first four Brillouin zone for a simple cubic lattice in two dimensions. Show that for a simple square lattice the kinetic energy of a free electron at the corner of the first Brillouin zone is double than that of an electron at the centre of the side face of the zone.
23. (a) Describe the basic nuclear properties and explain how nuclear forces can be accounted for by liquid drop model.
- (b) Point out validity and limitations of single particle shell model.
24. (a) What is a compound nucleus ? Discuss Bohr's theory of compound nucleus.
- (b) By giving necessary reactions explain how the neutrons are produced. What is the significance of neutron sources ?
25. Discuss Fermi theory of β -decay to explain the β -spectral shapes. What is non-conservation of parity ? Describe how this was established by an experiment on β -decay.
26. (a) Give in brief the classification of fundamental forces and elementary particles.
- (b) State the significance of the quadruple moment of a nucleus and obtain expression for this quantity.

Q. No.